

$$E_{\text{outside tangential}} - E_{\text{inside tangential}} = 0$$

$$B_{\text{outside tangential}} - B_{\text{inside tangential}} = 0$$

$$E_{\text{outside tangential}} = E_{\text{inside tangential}}$$

$$B_{\text{outside tangential}} = B_{\text{inside tangential}}$$

Tangential components of both  $E$  and  $B$  are continuous at the boundary.

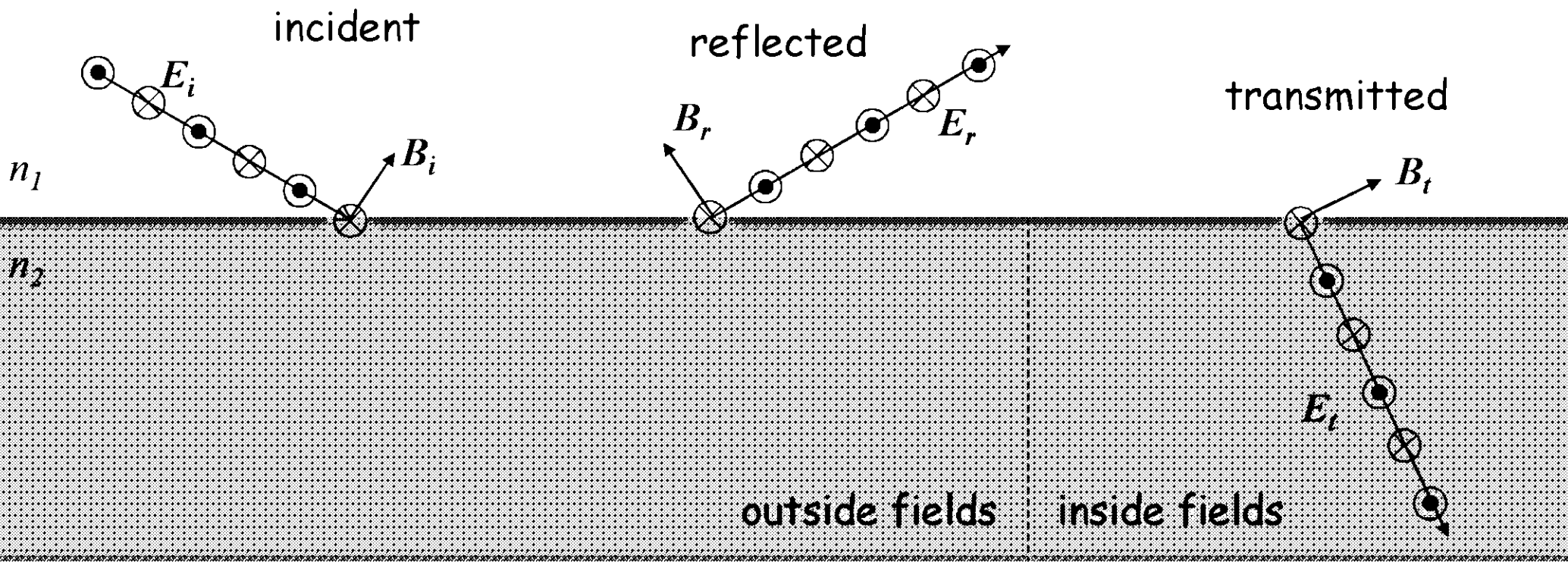
Therefore, for all points on the boundary at all times:

$$\vec{E}_{oi} e^{j\phi_i} e^{j(\vec{k}_i \cdot \vec{r} - \omega_i t)} + \vec{E}_{or} e^{j\phi_r} e^{j(\vec{k}_r \cdot \vec{r} - \omega_r t)} = \vec{E}_{ot} e^{j\phi_t} e^{j(\vec{k}_t \cdot \vec{r} - \omega_t t)}$$

(Tangential components)

Now for the relative amplitudes: TE reflection

$$r_{TE} = \frac{E_r}{E_i}$$



Tangential fields  
must be continuous:

$$E_i + E_r = E_t$$

$$B_i \cos \theta_i - B_r \cos \theta_r = B_t \cos \theta_t$$

The amplitudes are related by the velocity in the medium:

$$E = vB = \left(\frac{c}{n}\right)B$$

$$E_i = \left(\frac{c}{n_1}\right)B_i \quad E_r = \left(\frac{c}{n_1}\right)B_r \quad E_t = \left(\frac{c}{n_2}\right)B_t$$

Re-write the  $B$  continuity equation in terms of  $E$  (the  $c$ 's cancel and  $\theta_i = \theta_r$ ):

$$n_1 E_i \cos \theta_i - n_1 E_r \cos \theta_i = n_2 E_t \cos \theta_t$$

Combine this version of the  $B$  continuity and  $E$  continuity to eliminate  $E_t$ :

$$n_1 E_i \cos \theta_i - n_1 E_r \cos \theta_i = n_2 (E_i + E_r) \cos \theta_t$$

Solve this for  $E_r/E_i$  to get the reflection coefficient:

$$E_i (n_1 \cos \theta_i - n_2 \cos \theta_t) = E_r (n_2 \cos \theta_t + n_1 \cos \theta_i)$$

$$r_{TE} = \frac{E_r}{E_i} = \frac{(n_1 \cos \theta_i - n_2 \cos \theta_t)}{(n_2 \cos \theta_t + n_1 \cos \theta_i)}$$

Combine  $n_1$  and  $n_2$  into the relative index  $n = n_2/n_1$

$$r_{TE} = \frac{(\cos \theta_i - n \cos \theta_t)}{(\cos \theta_i + n \cos \theta_t)}$$

Convert  $\cos(\theta_t)$  to sine and use Snell's law to get rid of  $\theta_t$ :

$$r_{TE} = \frac{\cos \theta_i - n \sqrt{1 - \sin^2 \theta_t}}{\cos \theta_i + n \sqrt{1 - \sin^2 \theta_t}} = \frac{\cos \theta_i - n \sqrt{1 - \frac{1}{n^2} \sin^2 \theta_i}}{\cos \theta_i + n \sqrt{1 - \frac{1}{n^2} \sin^2 \theta_i}}$$

$$r_{TE} = \frac{\cos \theta_i - \sqrt{n^2 - \sin^2 \theta_i}}{\cos \theta_i + \sqrt{n^2 - \sin^2 \theta_i}}$$