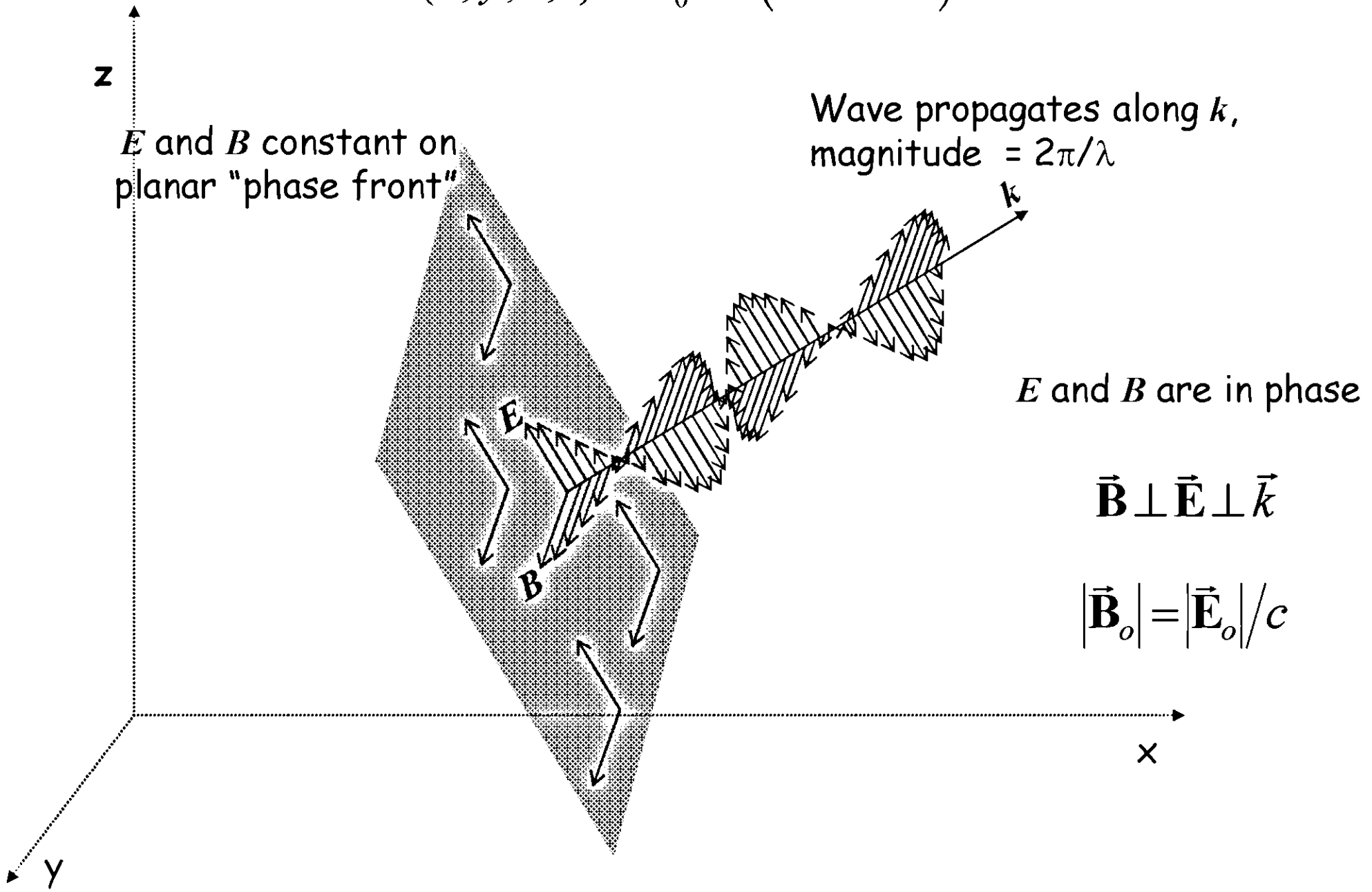


EM Plane Wave: $\vec{E}(x, y, z, t) = \vec{E}_0 \sin(\vec{k} \cdot \vec{r} - \omega t)$
 $\vec{B}(x, y, z, t) = \vec{B}_0 \sin(\vec{k} \cdot \vec{r} - \omega t)$



Energy density (J/m³) in an electrostatic field:

$$u_E = \frac{1}{2} \epsilon_0 E^2$$

Energy density (J/m³) in a magnetostatic field:

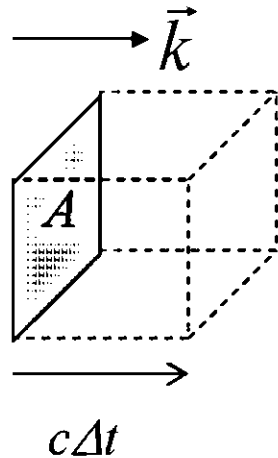
$$u_B = \frac{1}{2\mu_0} B^2$$

Energy density in an electromagnetic wave is equally divided:

$$\begin{aligned} u_E &= \frac{1}{2} \epsilon_0 E^2 \\ &= \frac{1}{2} \epsilon_0 c^2 B^2 \\ &= \frac{\epsilon_0}{2\epsilon_0\mu_0} B^2 \\ &= u_B \end{aligned}$$

$$u_{total} = u_E + u_B = \epsilon_0 E^2 = \frac{1}{\mu_0} B^2$$

Rate of energy transport: Power (W)



$$P = \frac{\text{energy}}{\Delta t} = \frac{u\Delta V}{\Delta t} = \frac{uAc\Delta t}{\Delta t}$$

$$P = ucA$$

Power per unit area (W/m²):

$$S = uc$$

$$S = \epsilon_0 c^2 EB$$

$$\vec{S} = \epsilon_0 c^2 \vec{E} \times \vec{B}$$

~~Pointing~~ Vector

Poynting

Poynting Vector oscillates very rapidly!

$$E = E_0 \cos(\omega t) \quad B = B_0 \cos(\omega t)$$

$$S = \varepsilon_0 c^2 E_0 B_0 \cos^2(\omega t)$$

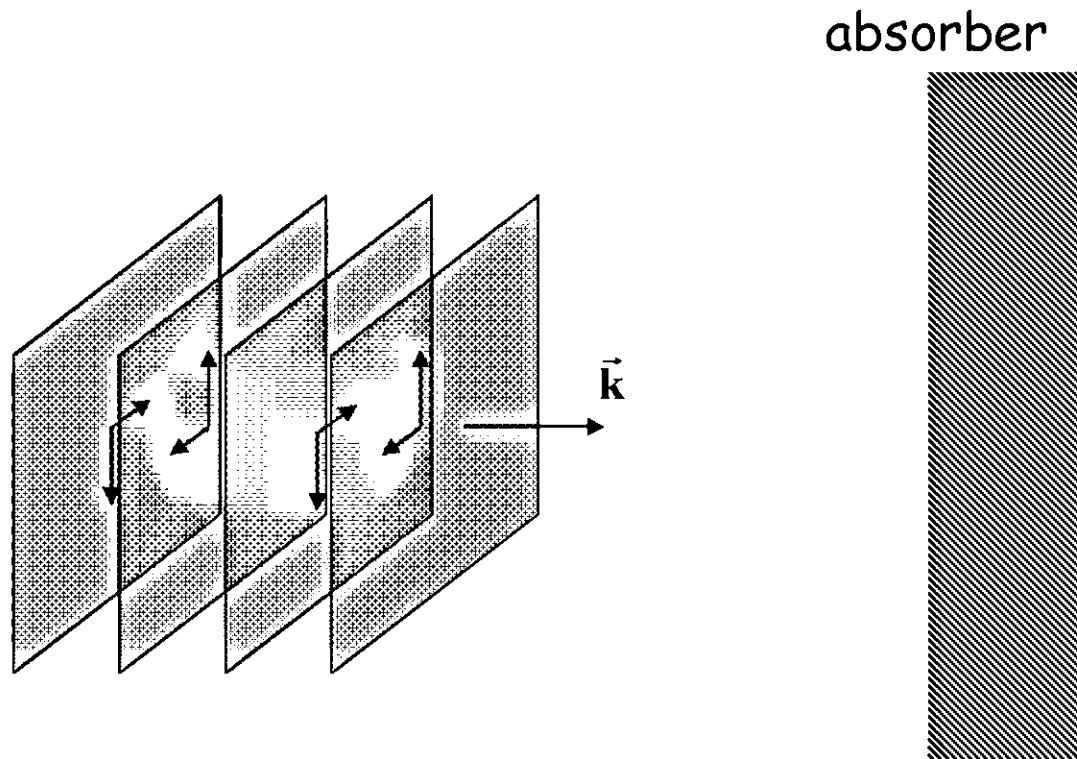
Take the time average:

$$\langle S \rangle = \varepsilon_0 c^2 E_0 B_0 \overline{\cos^2(\omega t)}$$

$$\langle S \rangle = \frac{1}{2} \varepsilon_0 c^2 E_0 B_0$$

$$\langle S \rangle = E_e \quad \text{"Irradiance" (W/m}^2\text{)}$$

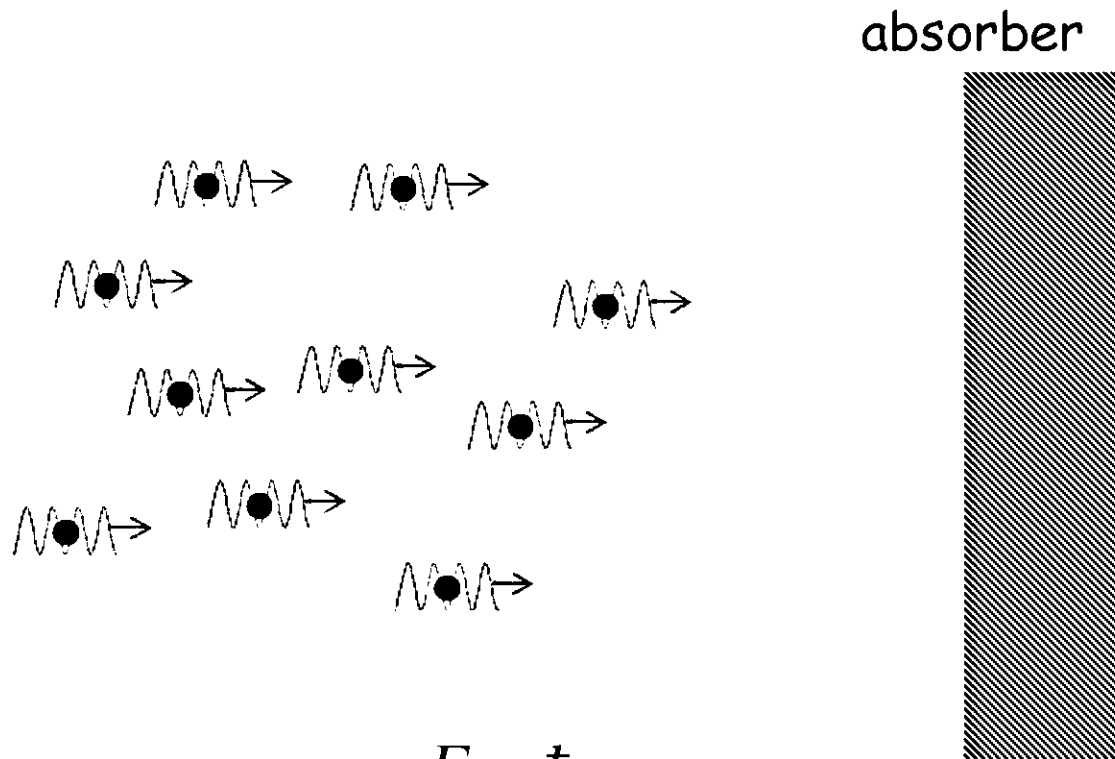
EM radiation carries momentum:



Radiation pressure $P = u_{total} = \frac{\vec{S}}{c}$

$$\langle P \rangle = \frac{E_e}{c}$$

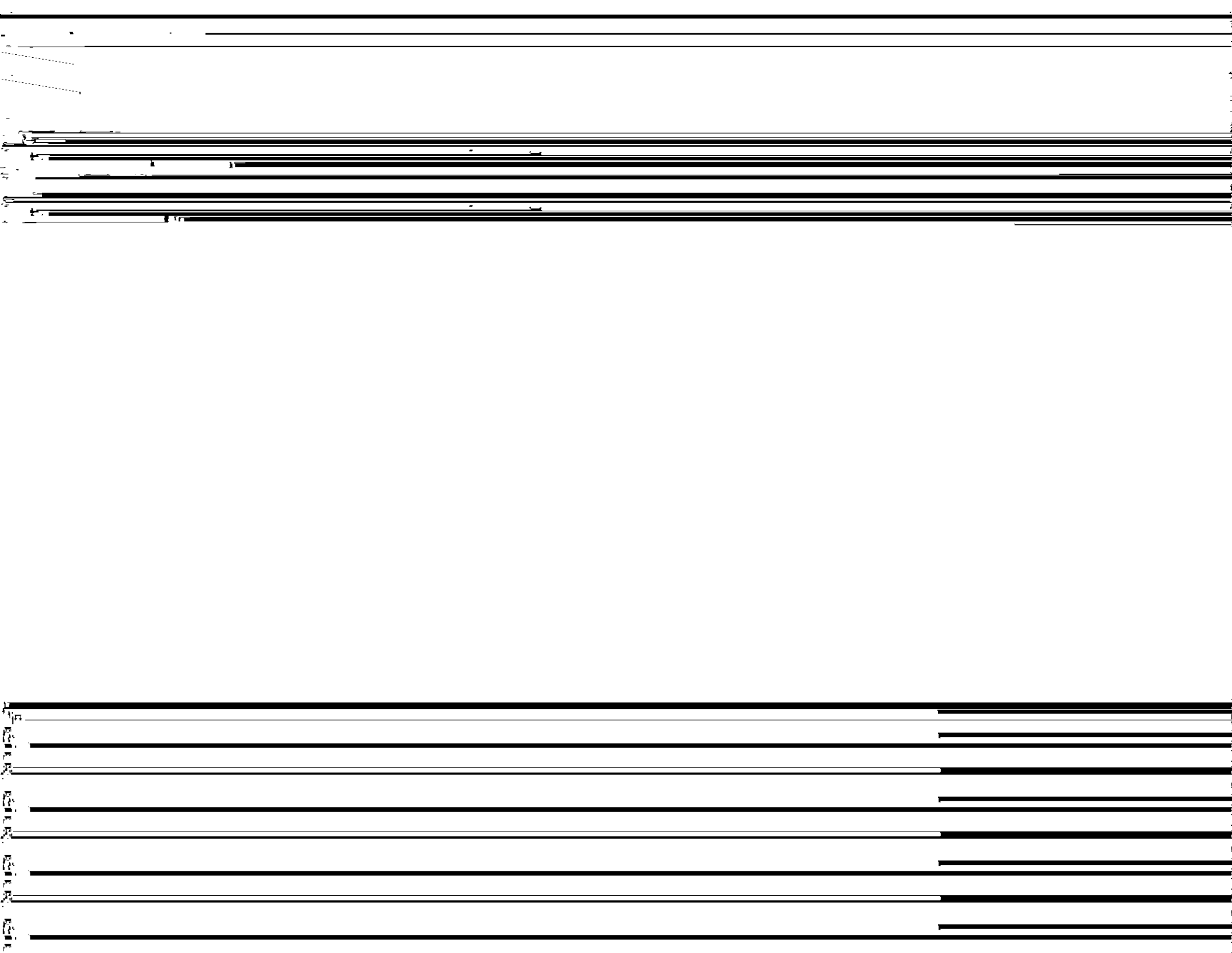
Light is really made up of particles - photons



They carry energy: $E = \hbar\omega$

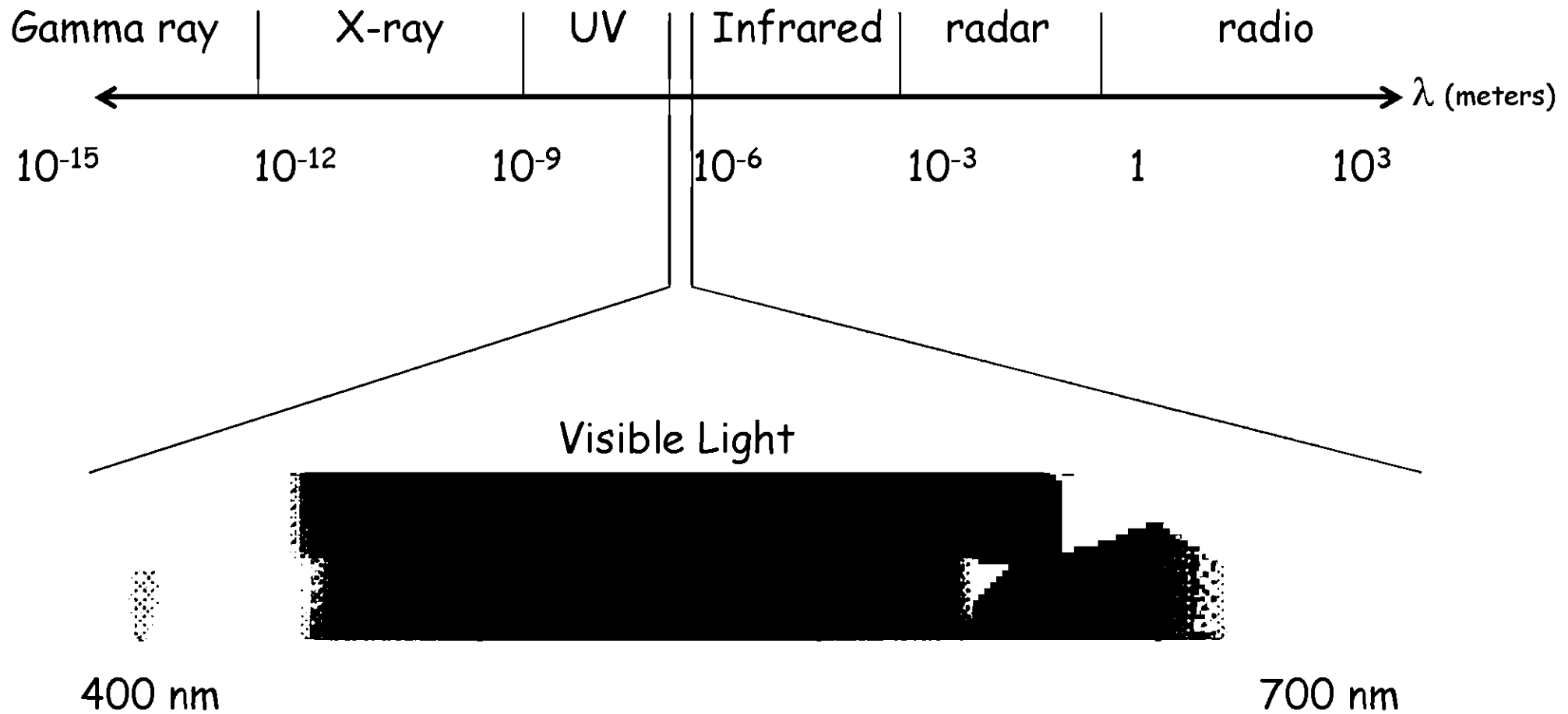
and momentum: $p = \hbar k$

"H-bar" is Planck's constant: $\hbar = 1.05 \times 10^{-34} \text{ Js}$



$$\vec{E}(\vec{r}, t) = \vec{E}_0 \cos(\vec{k} \cdot \vec{r} - \omega t)$$

$$\omega = ck$$



Photometry: the measurement of EM radiation *as perceived by the eye*.

Luminous Flux	Φ_v	lumen (lm)
Luminous Exitance	M_v	lm/m ²
Illuminance	E_v	lm/m ² or lux (lx)
Luminous Intensity	I_v	lm/sr or candela (cd)
Luminance (brightness)	L_v	cd/m ² or nit

$$(\text{Photometric value}) = 685 \times V(\lambda) \times (\text{radiometric value})$$