- 1. Jeffrey starts out at (0,0) facing in some direction. Each second, Jeffrey walks forward 1 unit, and then turns counterclockwise by 45°. When Jeffrey returns to his starting point, what is the area of the shape he has made.
- 2. Pentagon ABCDE is inscribed in a circle of radius 1. If  $\angle DEA \cong \angle EAB \cong \angle ABC$ ,  $m \angle CAD = 60^{\circ}$ , and BC = 2DE, compute the area of ABCDE.
- 3. Let circle O have radius 5 with diameter  $\overline{AE}$ . Point F is outside circle O such that lines  $\overline{FA}$  and  $\overline{FE}$  intersect circle O at points B and D, respectively. If FA = 10 and  $m \angle FAE = 30^{\circ}$ , then the perimeter of quadrilateral ABDE can be expressed as  $a + b\sqrt{2} + c\sqrt{3} + d\sqrt{6}$ , where a, b, c, and d are rational. Find a + b + c + d.
- 4. Let  $\triangle ABC$  be equilateral. Two points D and E are on side BC (with order B, D, E, C), and satisfy  $\angle DAE = 30^{\circ}$ . If BD = 2 and CE = 3, what is BC?



- 5. Let ABCD be a cyclic quadrilateral with AB = 6, BC = 12, CD = 3, and DA = 6. Let E, F be the intersection of lines AB and CD, lines AD and BC respectively. Find EF.
- 6. Two parallel lines  $l_1$  and  $l_2$  lie on a plane, distance d apart. On  $l_1$  there are an infinite number of points  $A_1, A_2, A_3, \cdots$ , in that order, with  $A_n A_{n+1} = 2$  for all n. On  $l_2$  there are an infinite number of points  $B_1, B_2, B_3, \cdots$ , in that order and in the same direction, satisfying  $B_n B_{n+1} = 1$  for all n. Given that  $A_1 B_1$  is perpendicular to both  $l_1$  and  $l_2$ , express the sum  $\sum_{i=1}^{\infty} \angle A_i B_i A_{i+1}$  in terms of d.
- 7. In an unit square ABCD, find the minimum of  $\sqrt{2}AP + BP + CP$  where P is a point inside ABCD.
- 8. We have a unit cube ABCDEFGH where ABCD is the top side and EFGH is the bottom side with E below A, F below B, and so on. Equilateral triangle BDG cuts out a circle from the cube's inscribed sphere. Find the area of the circle.
- 9. Given  $\triangle ABC$ . Let A' lie on BC such that  $BA' = \frac{1}{4}A'C$ , B' lie on AC such that AB' = B'C, and C' lie on AB such that 2AC' = BC'. Let D be the point of intersection between AA' and CC', E the point of intersection between AA' and BB', and F the point of intersection between BB' and CC'. What is  $\frac{area(\triangle DEF)}{area(\triangle ABC)}$ ?
- 10. Given a triangle ABC with a = 5, b = 7, and c = 8, find the side length of the largest equilateral triangle PQR such that A, B, C lie on QR, RP, PQ respectively.